



Metrology for Climate Relevant VOCs

Dynamic reference gas mixture preparation and uncertainty: permeation and diffusion methods

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POLITECNICO
DI TORINO

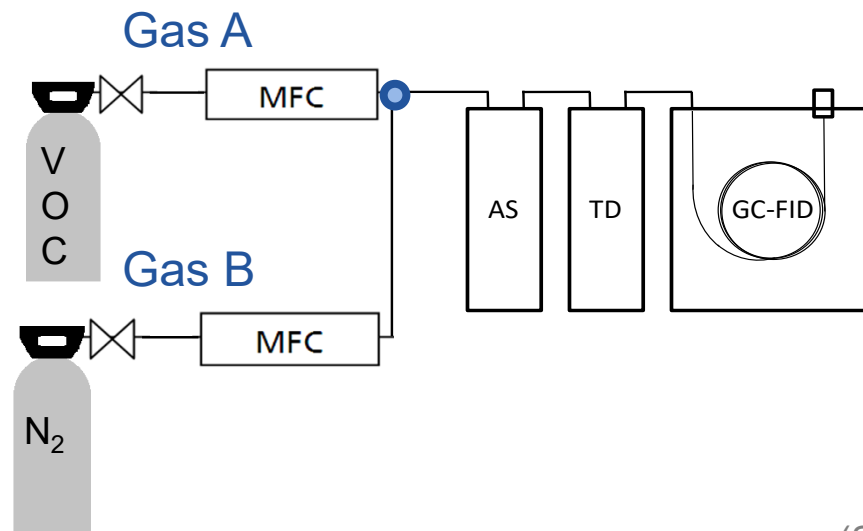


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ISO 6145 – dynamic methods

Preparation of calibration gas mixtures using dynamic methods, which rely in flow rates (gas A introduced at a known constant volume or mass flow rate into a known constant flow rate of gas B).

Dynamic dilution of a high fraction reference gas mixture with mass-flow controllers (MFCs)



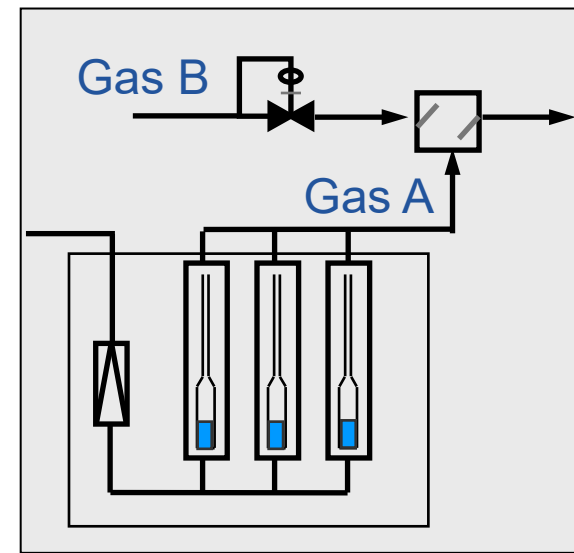
(Source: courtesy of VSL)

ISO 6145 – dynamic methods

Main dynamic methods

- Piston pumps
- Continuous injection
- Capillary
- Critical orifices
- Thermal mass-flow controllers
- **Diffusion**
- Saturation
- **Permeation**
- Electrochemical generation

Diffusion



(Source: courtesy of VSL)

Advantages and disadvantages

STATIC METHODS

VS.

DYNAMIC METHODS

- Wide range of concentrations.
- Un-tunability
- Suboptimal for unstable compounds
- Size and cost of cylinders
- Safety issues
- High minimal concentration
- Portability
- Limited long term stability

Advantages and disadvantages

STATIC METHODS

VS.

DYNAMIC METHODS

- Wide range of concentrations
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- Size and cost of cylinders
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- Wide range of concentrations
- Tunability
- Unstable compounds
- Long life low cost
- Safety issues
- Lower minimal concentration
- Low portability
- Long term stable



Permeation method

Permeation dynamic method: MSB



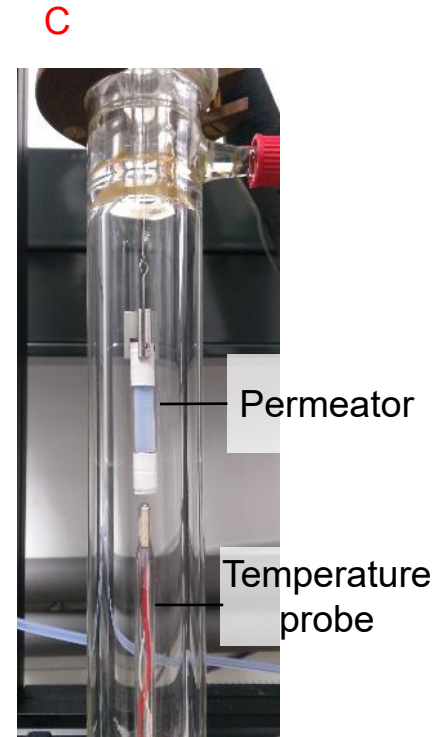
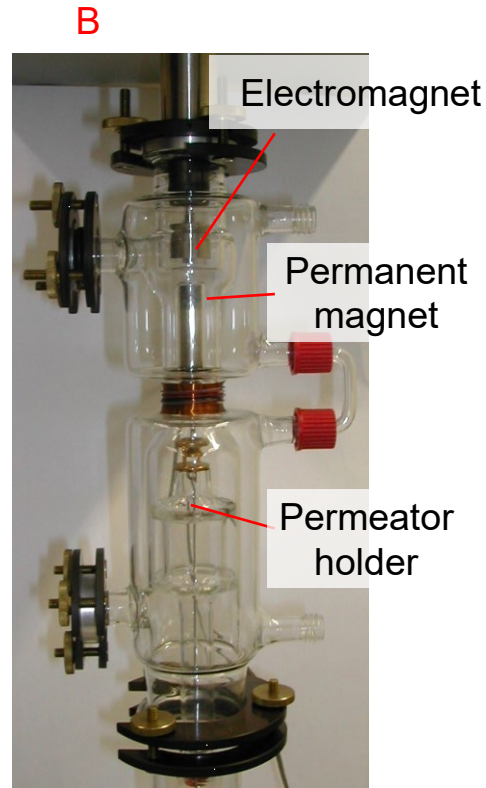
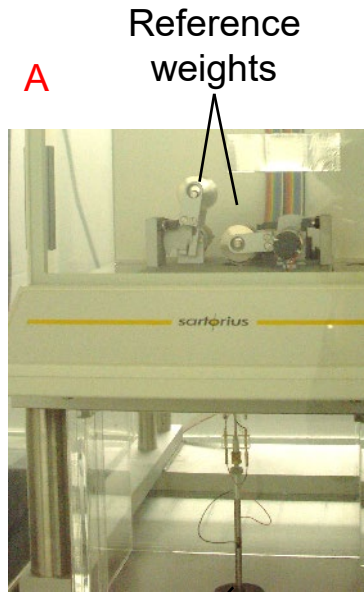
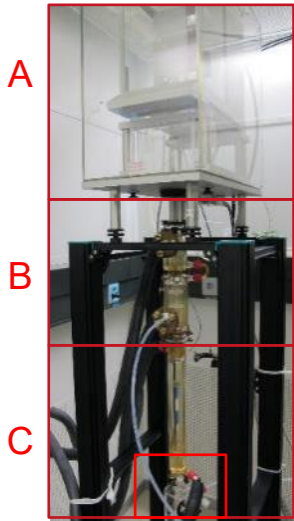
- TA Instruments (former Rubotherm)
- Glass/metal (SilcoNert 2000 coated SS)

Magnetic suspension balance (MSB):
glass (left), metal (right)

<https://www.metclimvoc.eu/training.html> (March 2021)

Permeation dynamic method: MSB

MSB elements



Electromagnet hanger

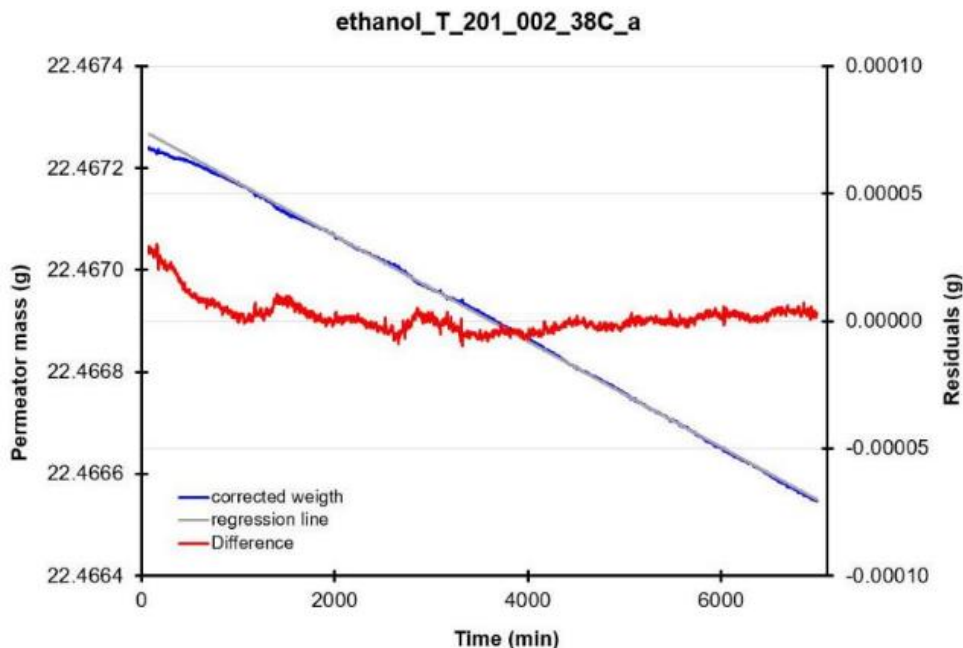
Mixing chamber

Permeation dynamic method: generation

Primary reference gas mixtures using a MSB (magnetic suspension balance)

Step 1: Calibration of the permeation unit

Controlled conditions (T, P, flow)

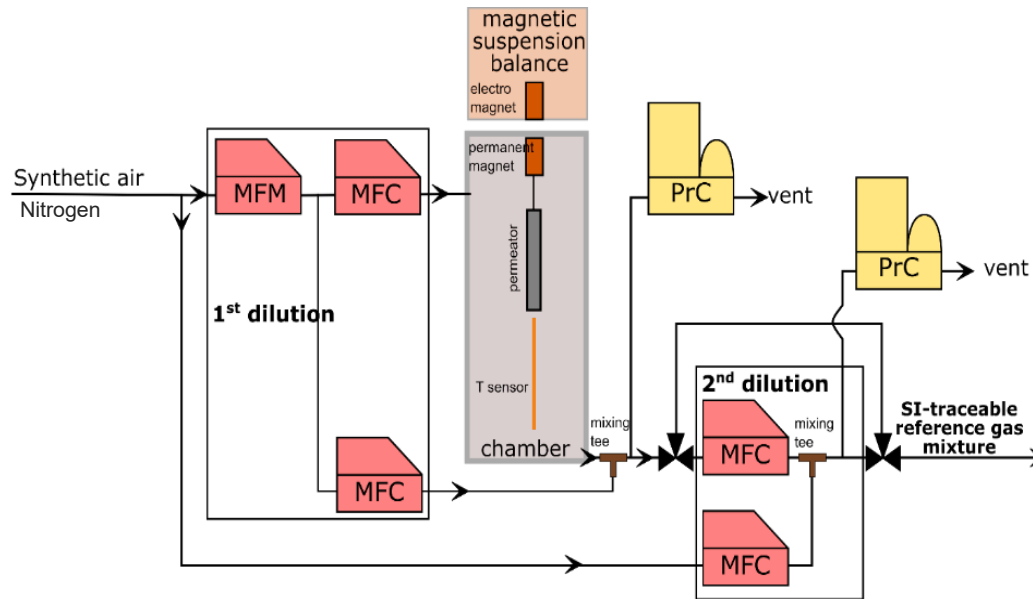


Permeation rate:

$$q_m = \frac{\Delta m}{\Delta t} = \frac{m_2 - m_1}{t_2 - t_1}$$

Permeation dynamic method: generation

Step 2: Dilution



$$1^{\text{st}} \text{ dilution: } X_{\text{RGM}} = q_m \cdot \text{purity} \cdot \left(\frac{V_{\text{mgas}}}{M_{\text{mcomp}}} \right) \cdot f_{\text{dil1}} + X_{\text{res}} \quad (> 30\text{-}50 \text{ nmol/mol})$$

$$2^{\text{nd}} \text{ dilution: } X_{\text{RGM}} = \left(q_m \cdot \text{purity} \cdot \left(\frac{V_{\text{mgas}}}{M_{\text{mcomp}}} \right) \cdot f_{\text{dil1}} + X_{\text{res}} \right) \cdot f_{\text{dil2}} + X_{\text{res}} \quad (< 30 \text{ nmol/mol})$$

Permeation dynamic method: uncertainty

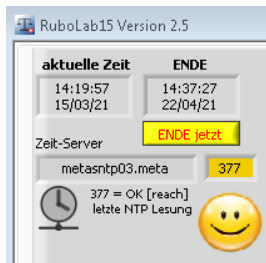
Main contributors to the uncertainty of the RGM amount fraction generated

$$X_{\text{RGM}} = q_m \cdot \text{purity} \cdot \left(\frac{V_{\text{m}_{\text{gas}}}}{M_{\text{m}_{\text{comp}}}} \right) \cdot f_{\text{dil1}} + X_{\text{res}}$$

Permeation rate (step 1)

$$q_m = \frac{\Delta m}{\Delta t}$$

- Balance sensitivity: < 1.5 % ($u(S) = 3 \cdot 10^{-5} \text{ g}$)
- Buoyancy variations: < 1 % ($u(b) < 3 \cdot 10^{-7} \text{ g}$)
- Chamber temperature variations: negligible ($u(T) < 0.00026 \text{ }^\circ\text{C}$)
- Chamber pressure variations: negligible ($u(P) < 0.002 \text{ hPa}$)
- Noise of the system > 75 % ($u(SC) < 0.004 \text{ }%$)



- PC time synchronized through a Network-Time-Protocol (NTP) server with the Swiss official time given by **atomic clocks** at METAS photonic, time and frequency lab (**negligible**; $u(t) < 1 \cdot 10^{-18} \text{ s}$)

- Others: leaks, wall reactions...

Permeation dynamic method: uncertainty

Main contributors to the uncertainty of the RGM amount fraction generated

$$X_{\text{compound}} = q_m \cdot \text{purity} \cdot \left(\frac{V_{\text{mgas}}}{M_{\text{mcomp}}} \right) \cdot f_{\text{dil1}} + X_{\text{res}}$$

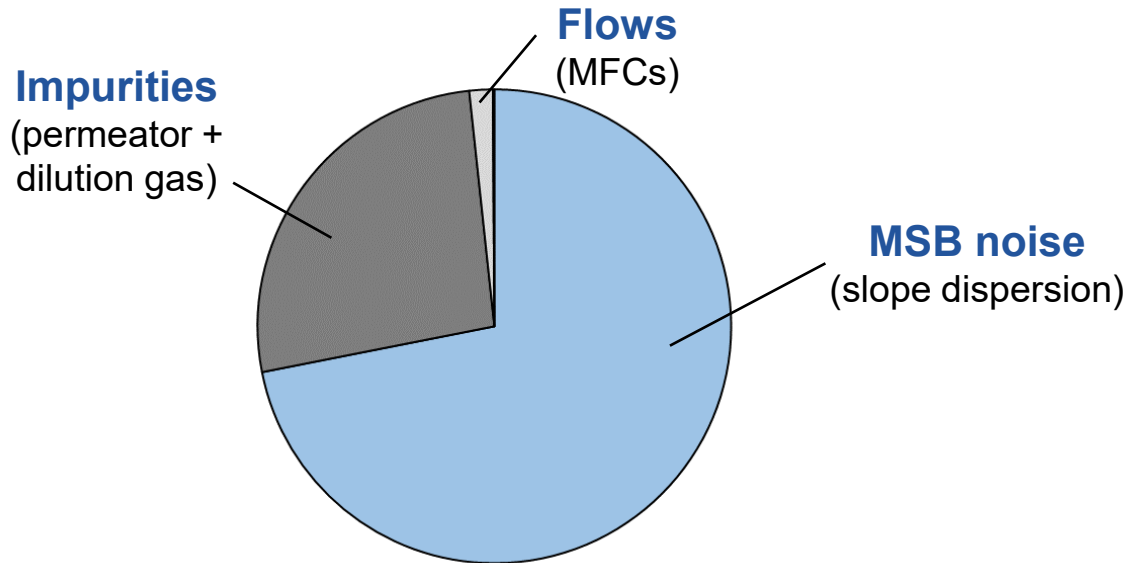
Step 2

- Impurities: variable
- Molar mass, molar volume: negligible (at 10^{-6} nmol/mol level)
- Dilution flow: 4-10 % ($u(q_v) < 0.2$ %)
- Residuals in dilution gas: variable
- Others: leaks, wall reactions...

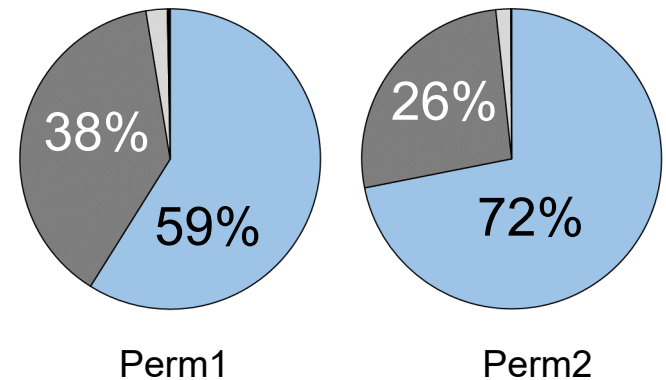
Permeation dynamic method: uncertainty

$$U(X_{RGM}) = k \cdot u_c(X_{RGM})$$

$$\frac{u_c(X_{RGM})}{X_{RGM}} = \sqrt{\left(\frac{u(q_m)}{q_m}\right)^2 + \left(\frac{u(q_v)}{q_v}\right)^2 + \dots +}$$



| Permeator | Dilution steps | Amount fraction (nmol/mol) | Uncertainty (k = 2) |
|-----------|----------------|----------------------------|---------------------|
| Perm1 | 2 | 31.3 | 1.9% |
| Perm2 | 1 | 345.9 | 1.6% |



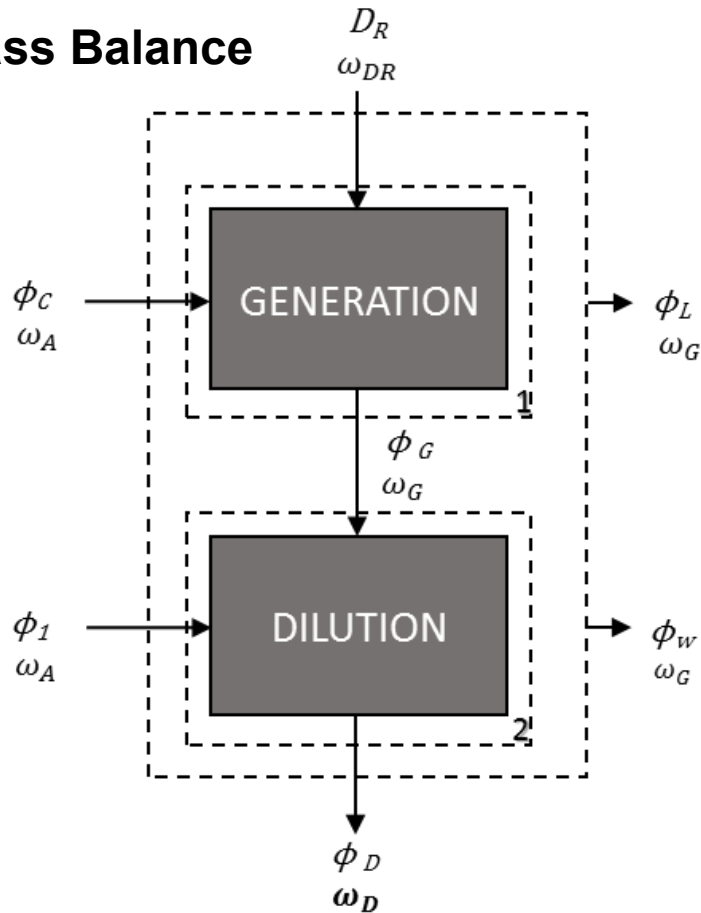


Diffusion method

Diffusion dynamic method

$P_v = 1-70 \text{ kPa @ generation T (26 } ^\circ\text{C)}$

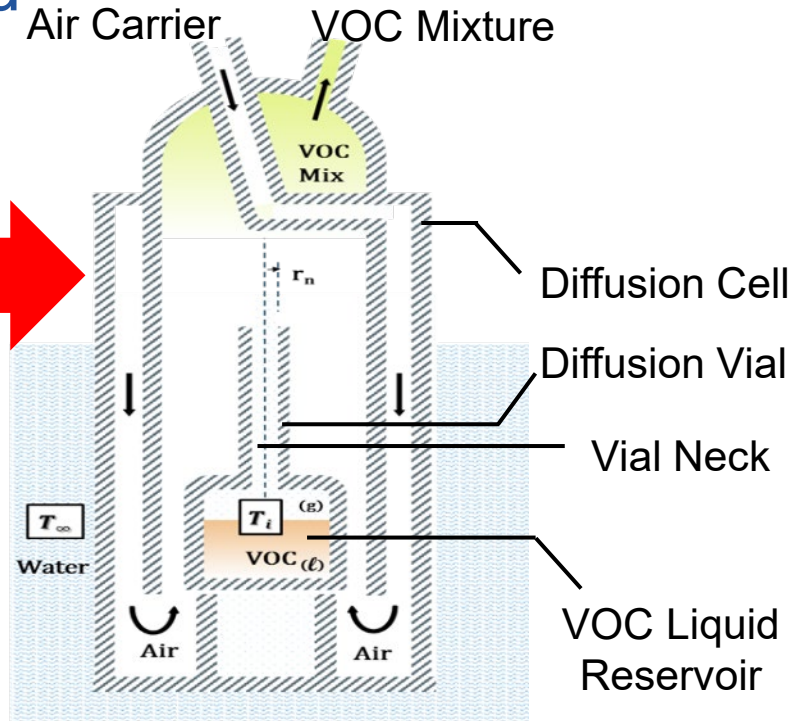
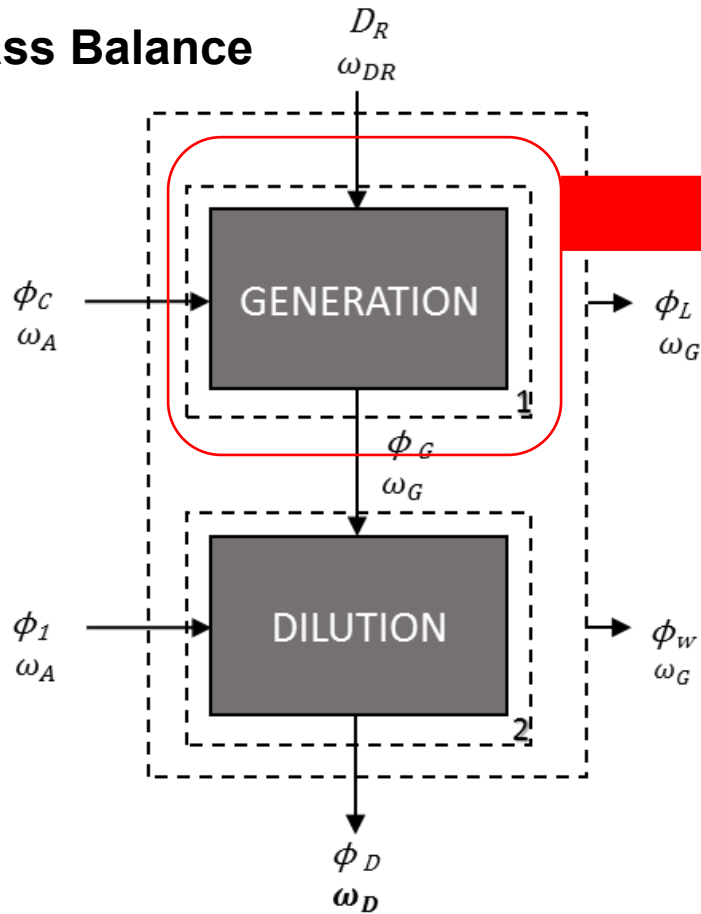
Mass Balance



- ✓ Fick's law of diffusion
- ✓ Perfect gas assumption
- ✓ Convective transport
- ✓ Turbulence for enhanced mixing

Diffusion dynamic method

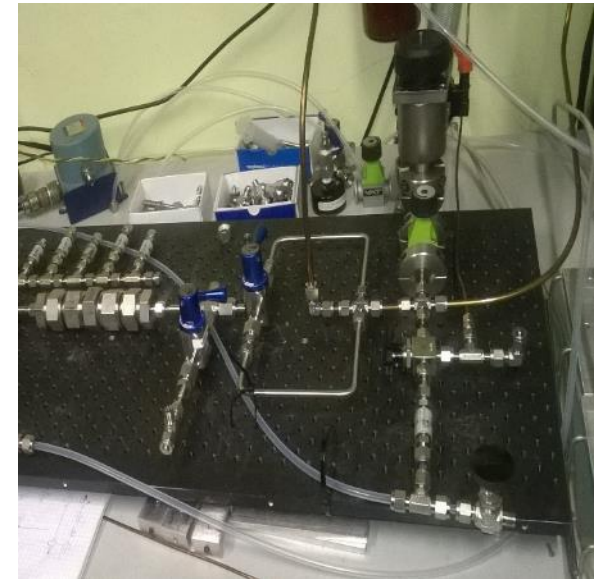
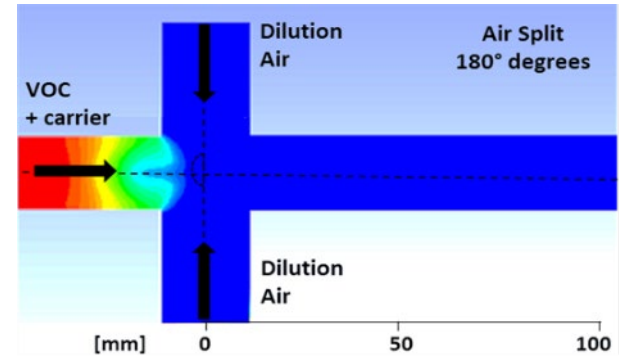
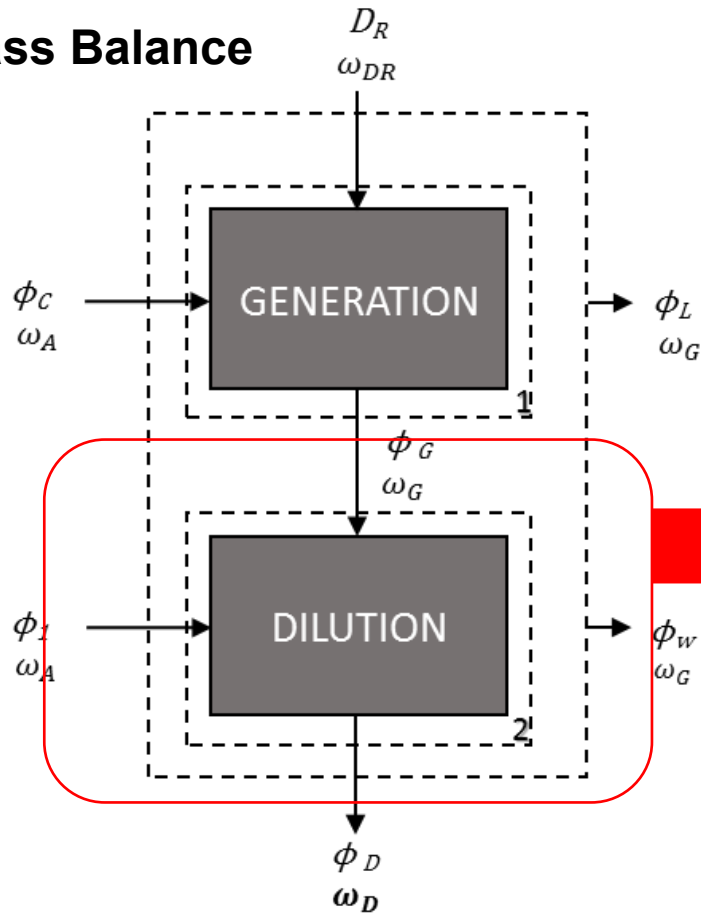
Mass Balance



Lecuna et al, 2018

Diffusion dynamic method

Mass Balance

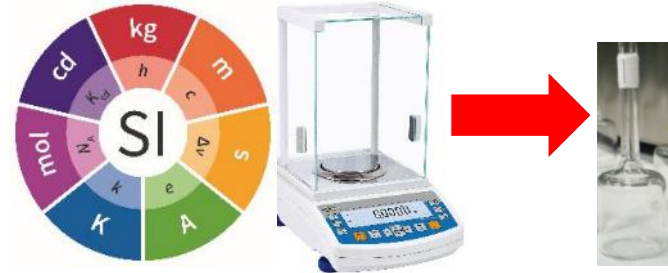


Sassi et al, 2015

Diffusion based - Primary device

Gravimetric Method

Primary = Directly traceable to SI (kg)



- ✓ **Average Diffusion rate**

$$D_{R,average} = \omega_{VOC} \left(\frac{\Delta m + \Delta m_B}{\Delta t} \right)$$

← **Mass evaporated (corrected for buoyancy) over a period of time**

- ✓ **Actual Pressure Correction**

$$D_{R,actual} = D_{R,average} \frac{\ln \left(1 - \frac{p_{VOC}}{p_{actual}} \right)}{\ln \left(1 - \frac{p_{VOC}}{p_{mean}} \right)}$$

← **Corrected to account for pressure variations**

Sassi et al, 2011

Diffusion rate Uncertainty

Propagation of uncertainty GUM JCGM 100:2008 (E) by BIPM

| X | [X] | x2 | u(x) | u%(x) | SI [%] |
|-----------------------|-----------------------------------|--------|----------|-------|---------|
| Δm | g | 0.01 | 3.81E-04 | 3.8% | 100.0% |
| Δt | days | 7 | 255 | 0.0% | 0.0% |
| p_{mean} | Pa | 98000 | 58 | 0.1% | 0.0% |
| p_{actual} | Pa | 101325 | 58 | 0.1% | 0.0% |
| p_{VOC} | Pa | 32154 | 643 | 3.0% | 0.0% |
| ω_{VOC} | g.g ⁻¹ | 1.0 | 0.0 | 0.1% | 0.0% |
| dp_{actual} | Pa | 0 | 50 | 0.0% | 0.0% |
| dT_{actual} | K | 0 | 0.02 | 0.0% | 0.0% |
| DR | $\mu\text{g}\cdot\text{min}^{-1}$ | 0.96 | 0.036 | 3.8% | (k = 1) |

Contribution to u(x)

$$C x_i = \left(\frac{df}{dx_i} \right)^2 u^2(x_i)$$

Significance Index (SI)

$$SI_i = \frac{C x_i}{\text{Max } C x_i}$$

$$u(x_{\text{VOC}}) = U(u(D_R), u(\phi_{\text{dilution}}))$$

Diffusion based - Working standard

Portable generation

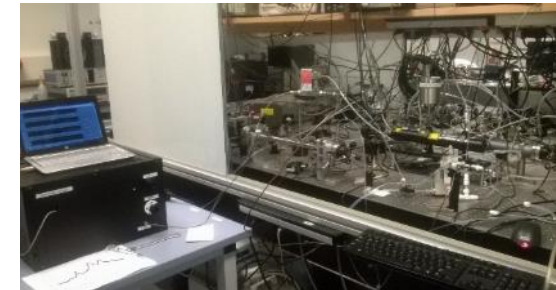
Working standard = Traceability to SI through a primary standard



**WORKING
STANDARD**



Transportable device in
INRIM (Italy)

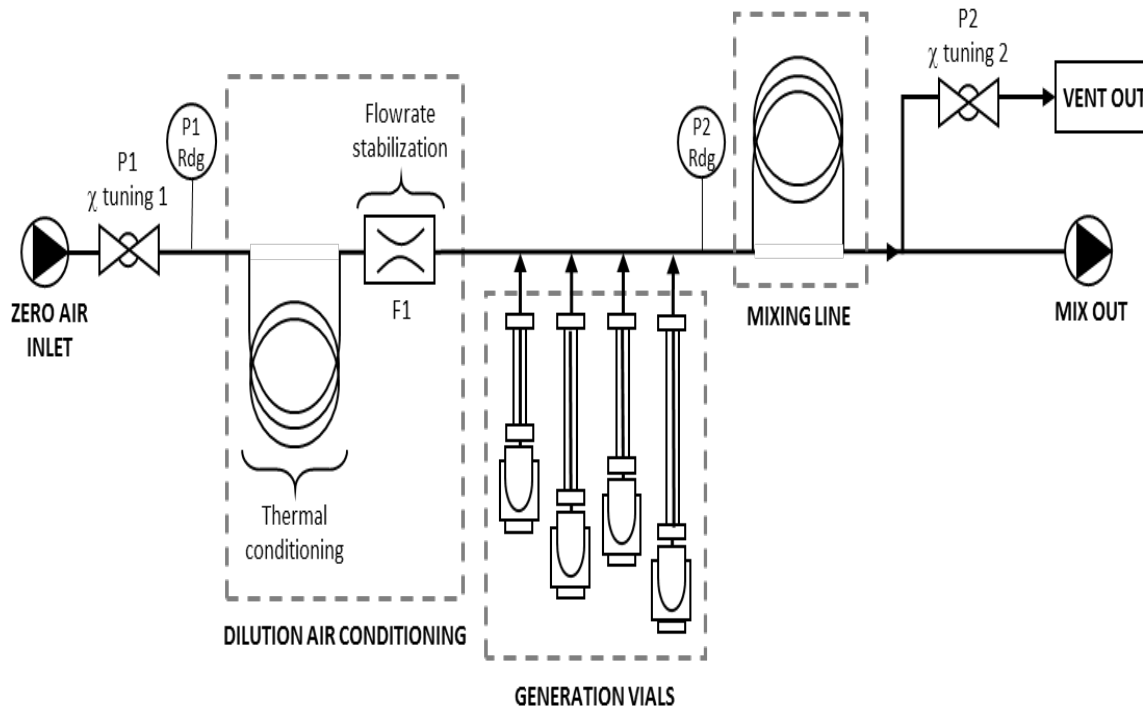


Transportable device in
VSL (Netherlands), 2017

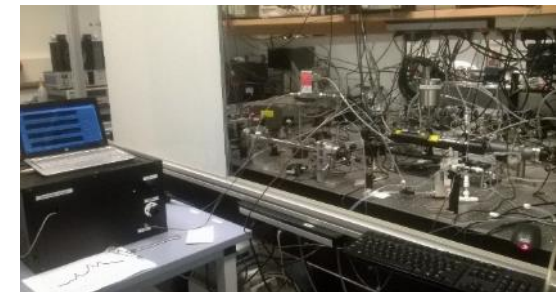
Diffusion based - Working standard

Portable generation

Working standard = Traceability to SI through a primary standard



Transportable device in INRIM (Italy)

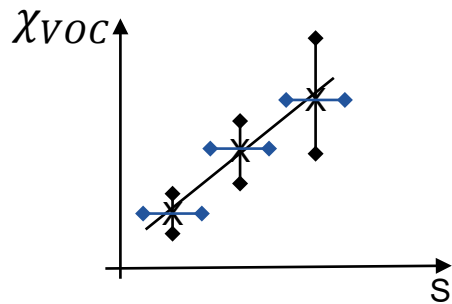


Transportable device in VSL (Netherlands), 2017

Demichelis et al, 2018

Working standard Calibration

Calibration curve of working standard, f



$$\chi_{VOC} = f(T, P, \phi_{dilution}, S)$$

**REFERENCE
GAS MIXTURE
(RGM)**



**UNKNOWN
AMOUNT
FRACTION
(WS)**

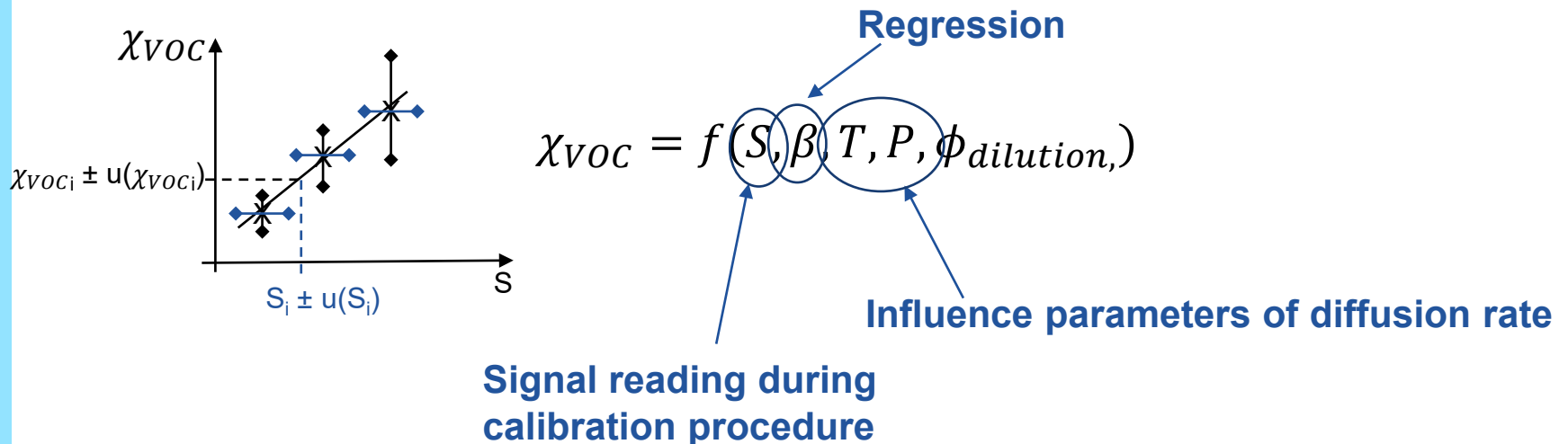


ANALYZER

**SIGNAL S_{RGM}
SIGNAL S_{WS}**

Working standard calibration

Calibration curve of working standard, f



Regression: Ordinary, Weighted, Weighted total depending on system

Uncertainty of regression: Algebraic or numerical (Montecarlo) approaches

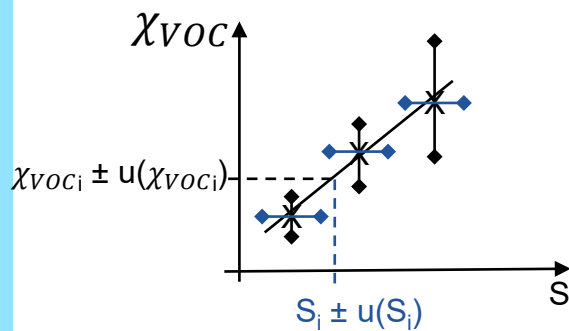
NMI reference software for regression:

CCC Software (INRIM) (Lecuna et al 2020)

XGENLINE/ XLGENLINE (NPL)

Amount fraction Uncertainty

Calibration curve of working standard, f



Regression

$$\chi_{VOC} = f(T, P, \phi_{dilution}, S)$$

Signal reading during calibration procedure

Influence parameters of diffusion rate

Uncertainty of the Calibration curve of working standard, f

$$U \chi_{VOC_{WS}}(T, P, \phi_{dilution}) = U(u(RGM), u(S), u(\beta_{regression}))$$



Metrology for Climate Relevant VOCs

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For more information, visit

www.metclimvoc.eu



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